

# SYNTHETIC GAUGE FIELDS FOR ULTRACOLD ATOMS IN SYNTHETIC DIMENSIONS

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# in collaboration with



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# Outlook

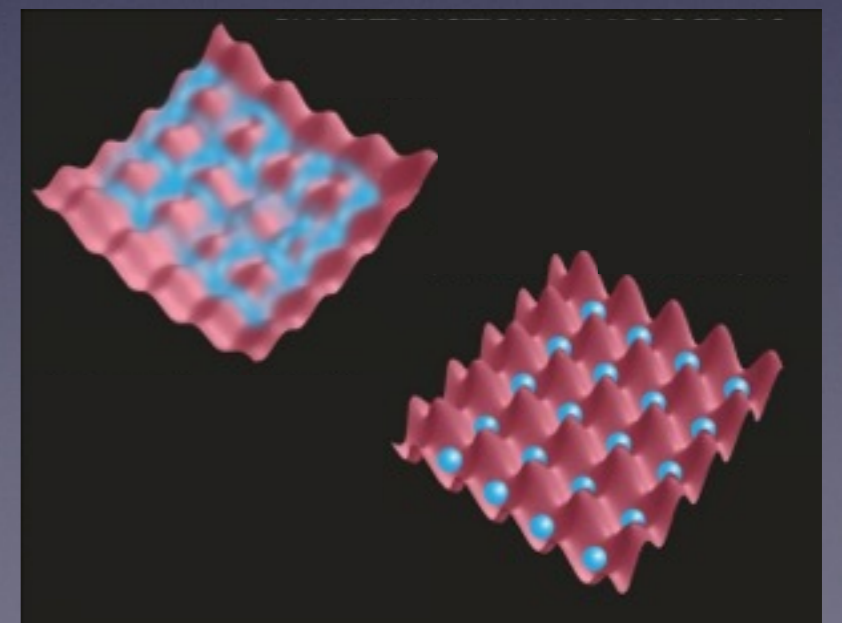
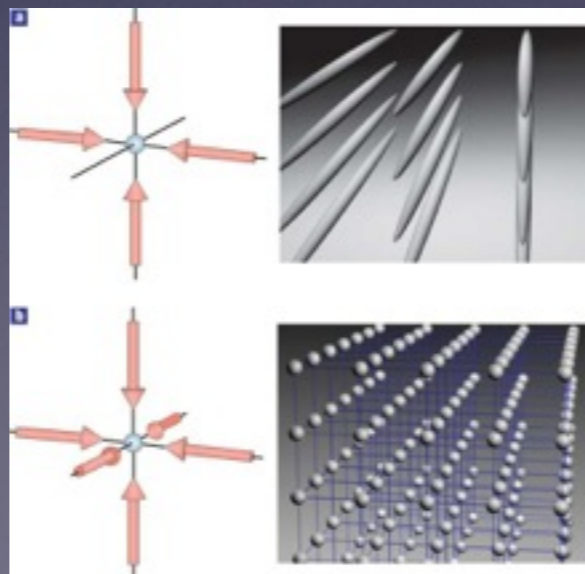
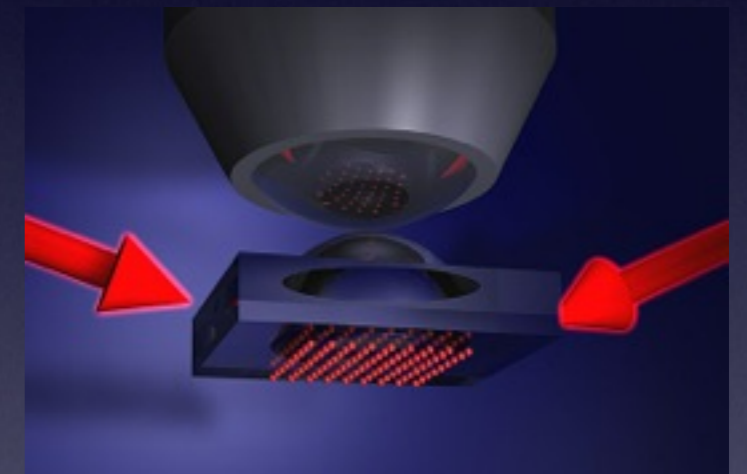
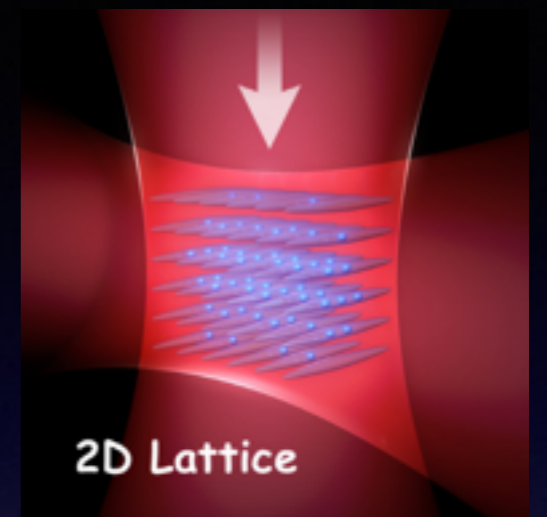
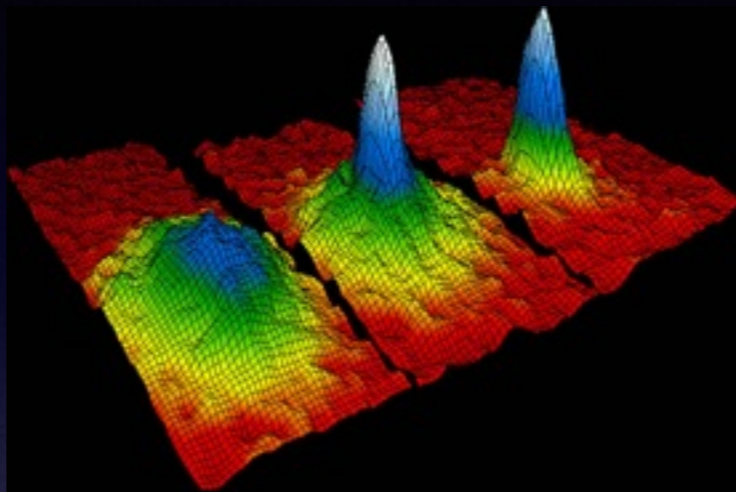
Ultracold quantum gases

Synthetic gauge fields

Synthetic dimensions

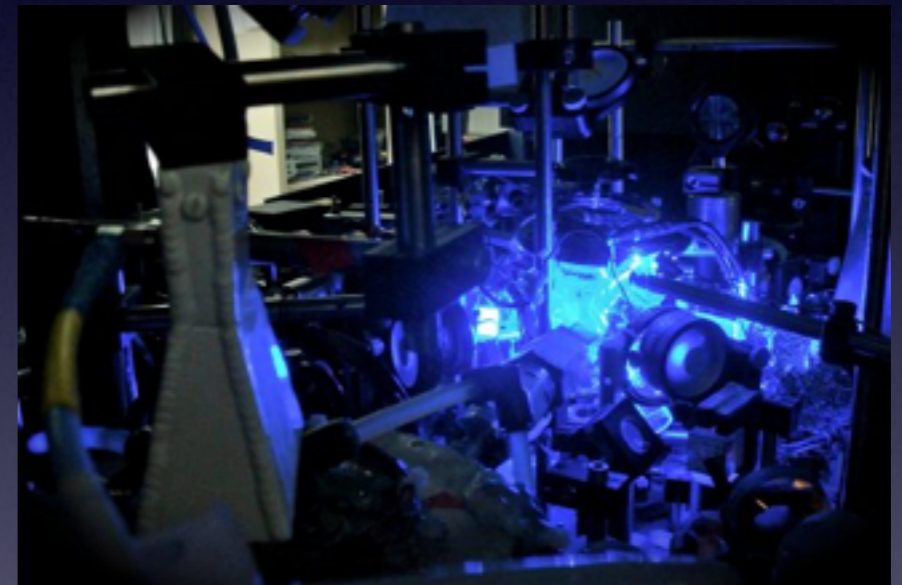
# Ultracold quantum gases

- neutral atoms ( $\sim$ alkali)
- bosons/fermions
- very dilute gas ( $d \sim \mu\text{m}$ )
- ultracold ( $T < T_c \sim 100\text{nK}$ )
- slow ( $E \sim \text{kHz}$ )
- isolated
- clean (but dopable)
- negligible spin-orbit coupling (but..)
- tuneable:
  - ★ chemical potential
  - ★ interactions
  - ★ geometries



# Ideal quantum playground

$$i\hbar\partial_t|\psi\rangle = (H_0 + H_{\text{int}} + H_{\text{so}} + \dots)|\psi\rangle$$



Topological states predicted in:

- fermionic p-wave superfluids\*
- 1D atomic chains in a superfluid bath
- fermionic s-wave superfluids in non-Abelian gauge fields\*\*
- ....

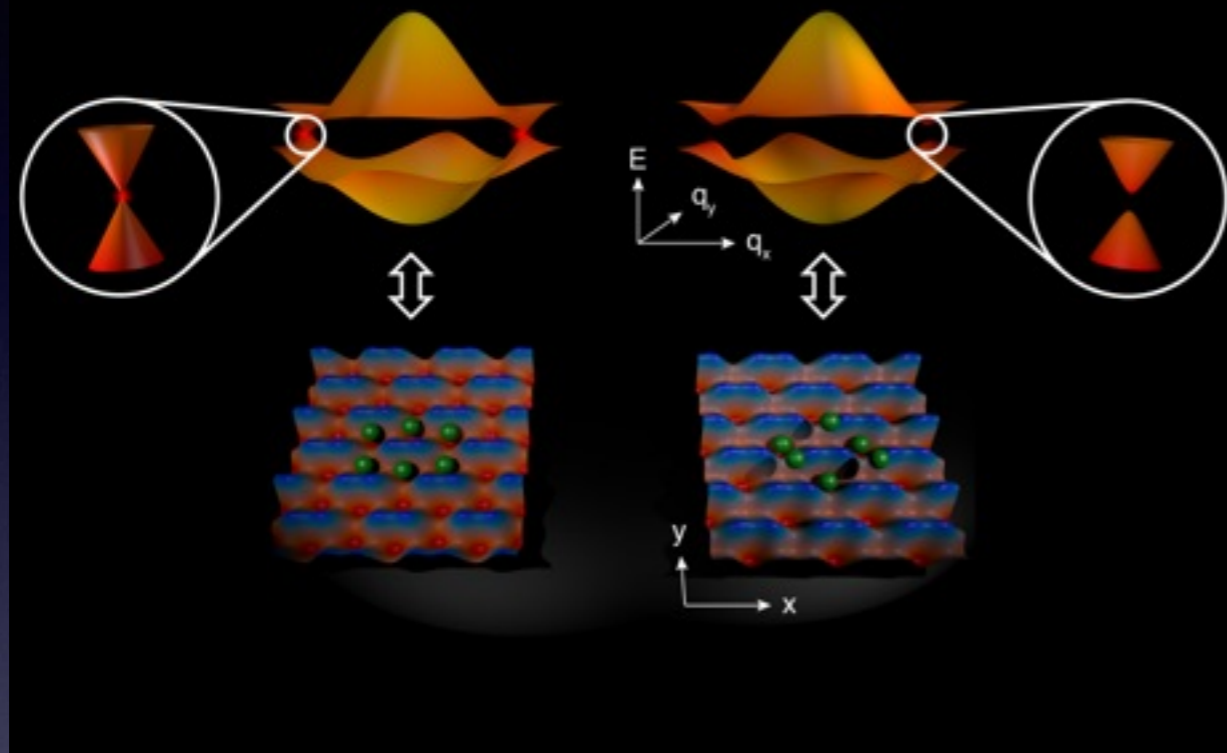
My contributions in these directions:

\* PM, Sanpera, and Lewenstein, PRA (2010)

\*\* Kubasiak, PM, and Lewenstein, EPL (2010)

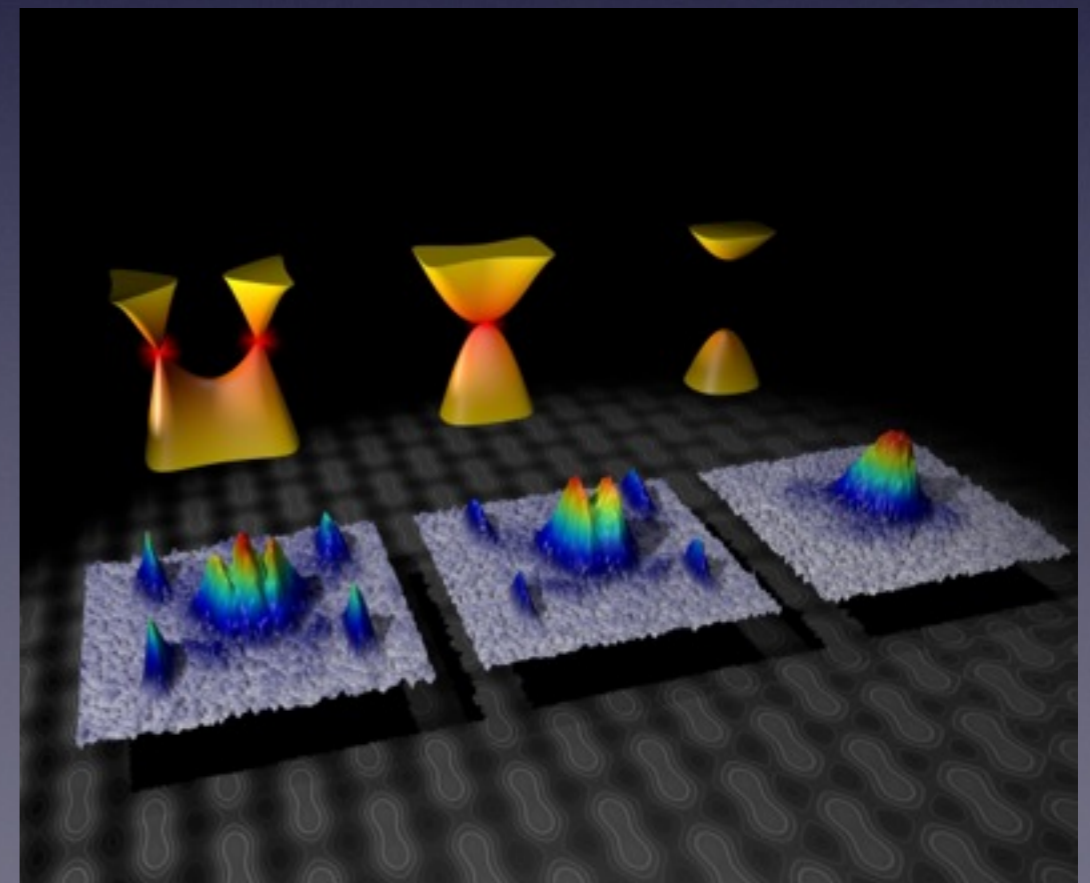
# Tuning the honeycomb

(a graphene emulator with variable lattice geometry)



- break A/B sublattice inversion symmetry makes Dirac fermions massive
- deform the lattice to displace, merge and annihilate pairs of Dirac cones

ETH group: Tarruell et al., Nature (2012)



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# Gauge fields in QM

Free space (minimal coupling):  $\frac{p^2}{2m} \longrightarrow \frac{(\mathbf{p} - e\mathbf{A})^2}{2m}$

Lattice (Peierls' subst.):  $-t \sum_{\langle n,m \rangle} a_{n+1,m}^\dagger a_{n,m} \longrightarrow -t \sum_{\langle n,m \rangle} e^{i\phi_{n,m}} a_{n+1,m}^\dagger a_{n,m}$

$$\phi_{n,m} = \frac{e}{\hbar} \int_{\mathbf{r}_{n,m}}^{\mathbf{r}_{n+1,m}} \mathbf{A} \cdot d\mathbf{s}$$

Problem: atoms are charge-neutral  
Solution: engineer synthetic ones?

Proposals: Jaksch&Zoller, NJP 2003  
Osterloh et al., PRL 2005  
... (and hundreds of papers more) ...

Methods:

- adiabatic Raman passage
- adiabatic control of superpositions of degenerate dark states
- spatially varying Raman coupling
- Raman-induced transitions to auxiliary states in optical lattices

REVIEWS:

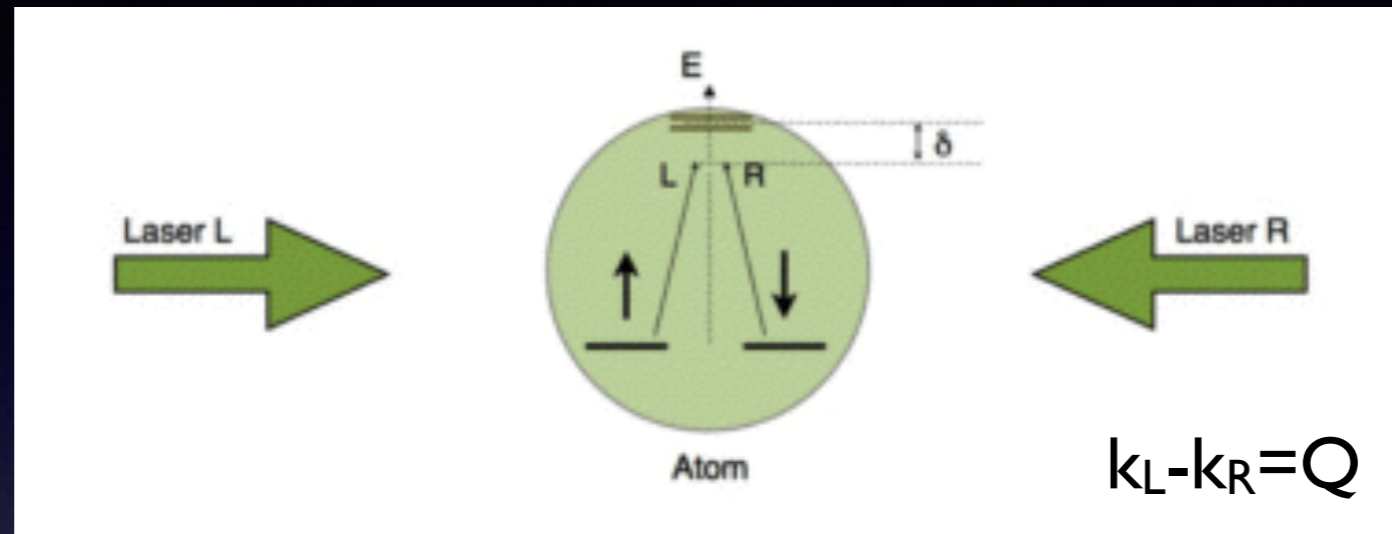
*Artificial gauge potentials for neutral atoms*  
Dalibard, Gerbier, Juzeliunas, and Öhberg, RMP (2011)

*Light-induced gauge fields for ultracold atoms*  
Goldman, Juzeliunas, Öhberg, and Spielman, arXiv (2014)  
(Rep. Prog. Phys., in press)



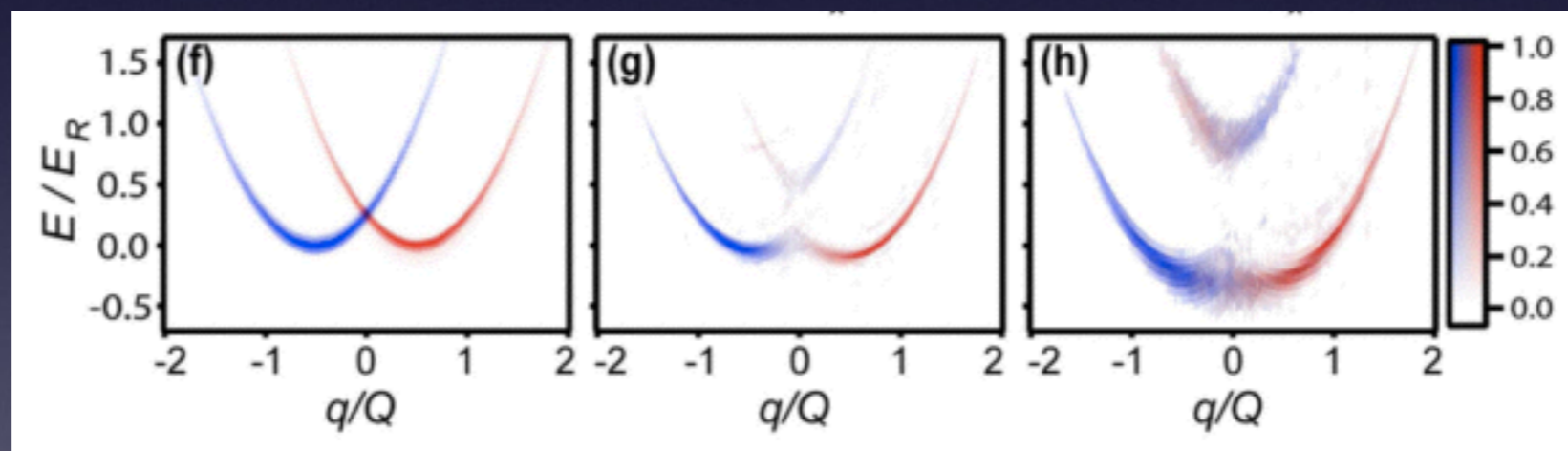
# Spin-orbit coupling for neutral atoms

off-resonant  
two-photon  
Raman transitions



$$|\uparrow, k_x - Q/2\rangle$$

$$|\downarrow, k_x + Q/2\rangle$$



increasing intensity of Raman lasers

spin flip  $\leftrightarrow$  momentum kick

Lin et al., Nature 2011 (JQI-NIST)  
P.Wang et al., PRL 2012 (Shanxi U.)  
L.W. Cheuk et al., PRL 2012 (MIT)

# Outlook

Ultracold quantum gases

Synthetic gauge fields

**Synthetic dimensions**

# Q. Sim. & Extra Dimensions

Quantum simulation with ultracold atoms:

- Hubbard model, MI/SF transition, ...
- relativistic dispersions, sonic black holes, ...
- strongly-correlated states (QH, spin liquids, ...)

Extra dimensions (=non-spatial):

- attempts to unify gravitation with electro-weak forces (Kaluza-Klein, Yang-Mills, ...)

- thermal QFT: compactification of euclidean time leads to

Matsubara frequencies

extra-dims are usually discrete and compact

quantum simulation of an extra dimension?

# The simple idea

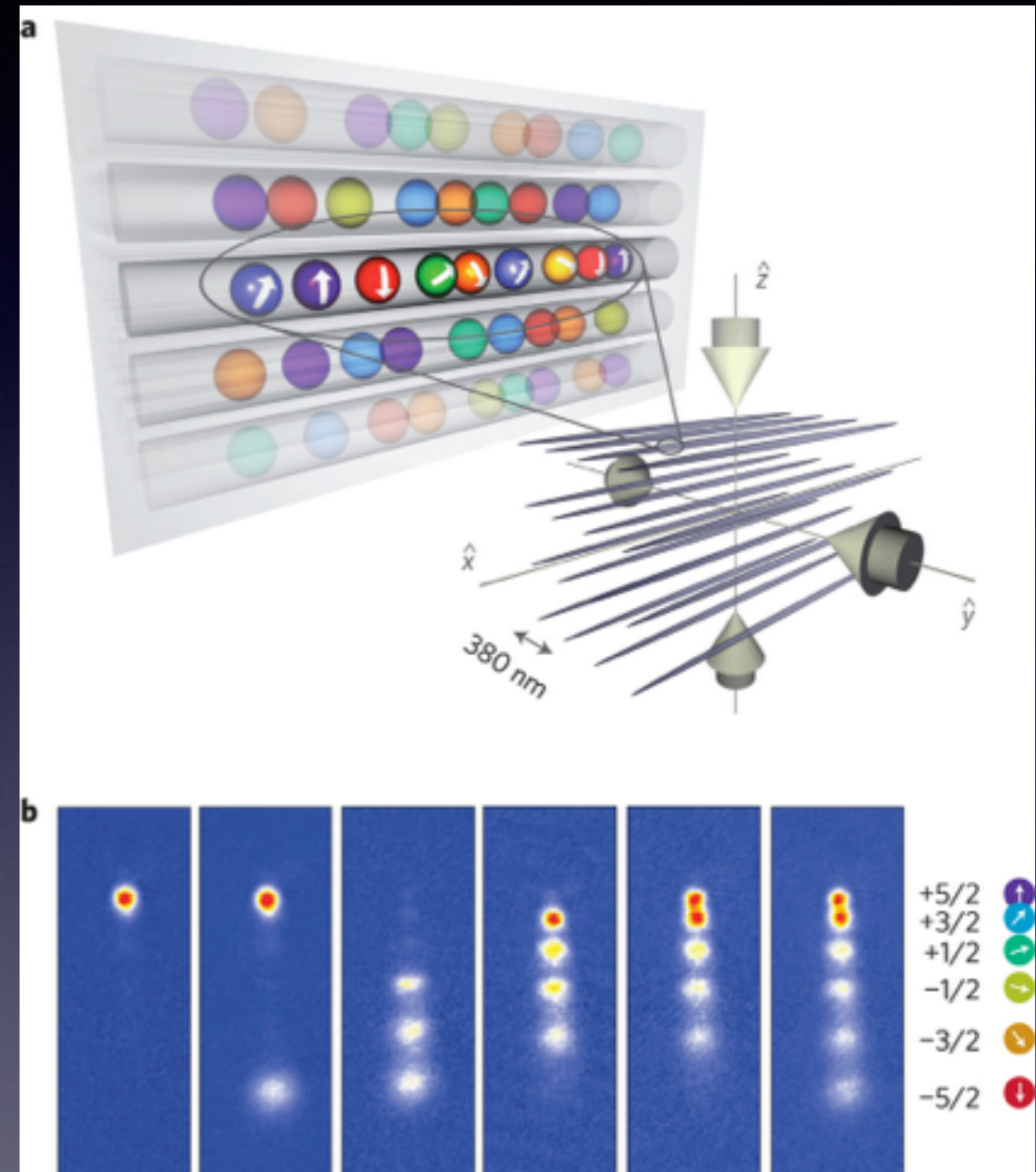
- use a system with  $D$  spatial dimensions
- encode the  $(D+1)^{\text{th}}$  dimension in an internal degree of freedom (e.g., the spin)

$$\begin{aligned}
 H &= - \sum_{d=1}^{D+1} \sum_{\tilde{\mathbf{r}}} J_d \hat{a}_{\tilde{\mathbf{r}}+\mathbf{u}_d}^\dagger \hat{a}_{\tilde{\mathbf{r}}} + \text{h.c.} & \tilde{\mathbf{r}} &= (\mathbf{r}, \sigma) \\
 &= - \sum_{\sigma=1}^N \left[ \sum_{d=1}^D \sum_{\mathbf{r}} \underbrace{J_d \hat{a}_{\mathbf{r}+\mathbf{u}_d}^{(\sigma)\dagger} \hat{a}_{\mathbf{r}}^{(\sigma)}}_{\substack{\text{usual hopping} \\ \text{(conserves spin)}}} + \underbrace{J_\sigma \hat{a}_{\mathbf{r}}^{(\sigma+1)\dagger} \hat{a}_{\mathbf{r}}^{(\sigma)}}_{\substack{\text{couple consecutive spin states} \\ \text{("spin hopping")}}} \right] + \text{h.c.}
 \end{aligned}$$

# Large N systems

species	N
Li	2,3,...
87	3
173	6
40	10
87	10
161-163	22

$^{173}\text{Yb}$  @ LENS:  
Pagano et al.  
Nat. Phys. (2014)



interactions in earth-alkali atoms are  $\text{SU}(N)$  invariant!

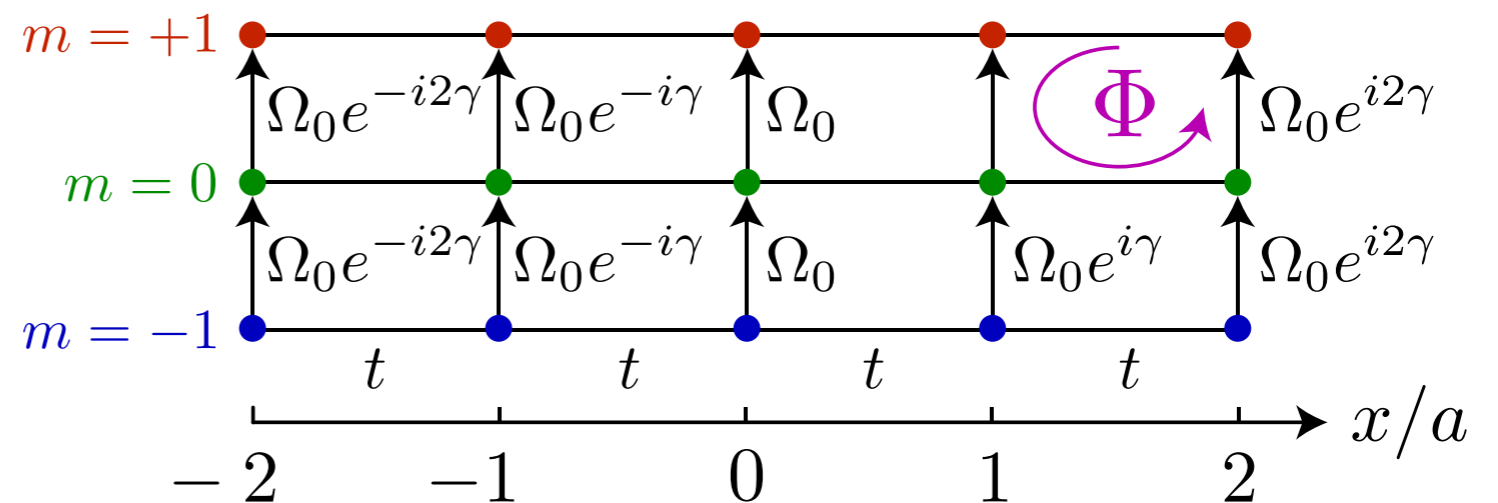
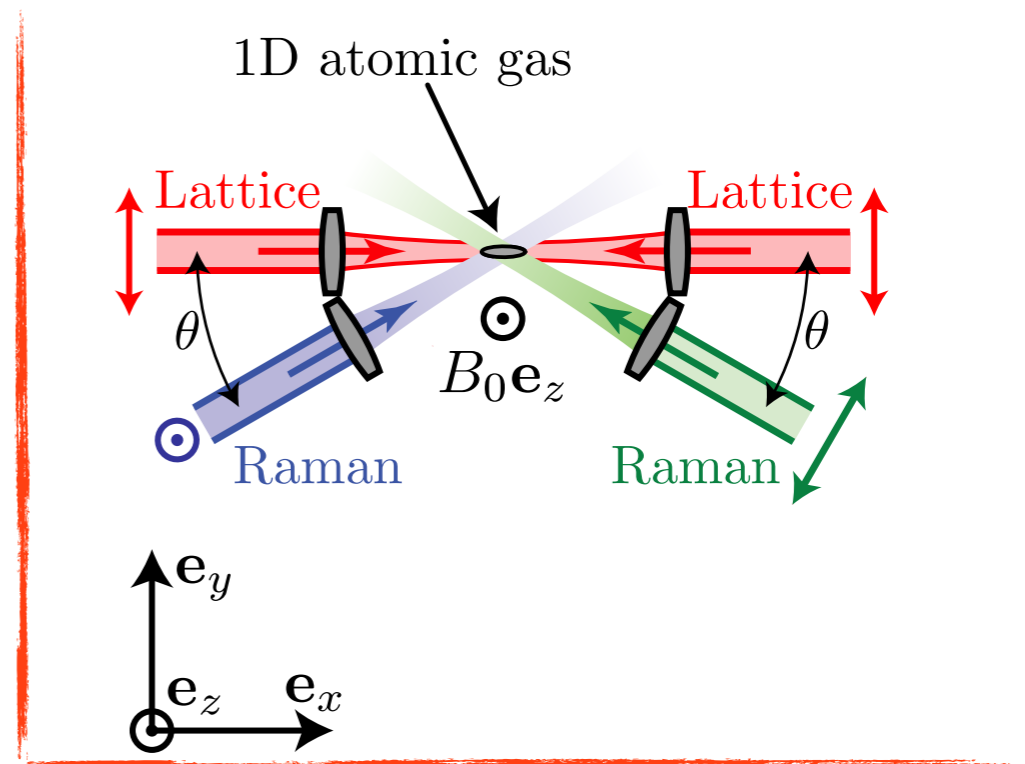
# Simplest implementation

Requires:

- atoms with three addressable internal states in a 1D optical lattice (e.g.,  $F=1$   $^{87}\text{Rb}$ )
- two  $\lambda_R$  Raman beams, providing recoil  $k_R = 2\pi \cos \theta / \lambda_R$
- uniform B-field in the z-direction

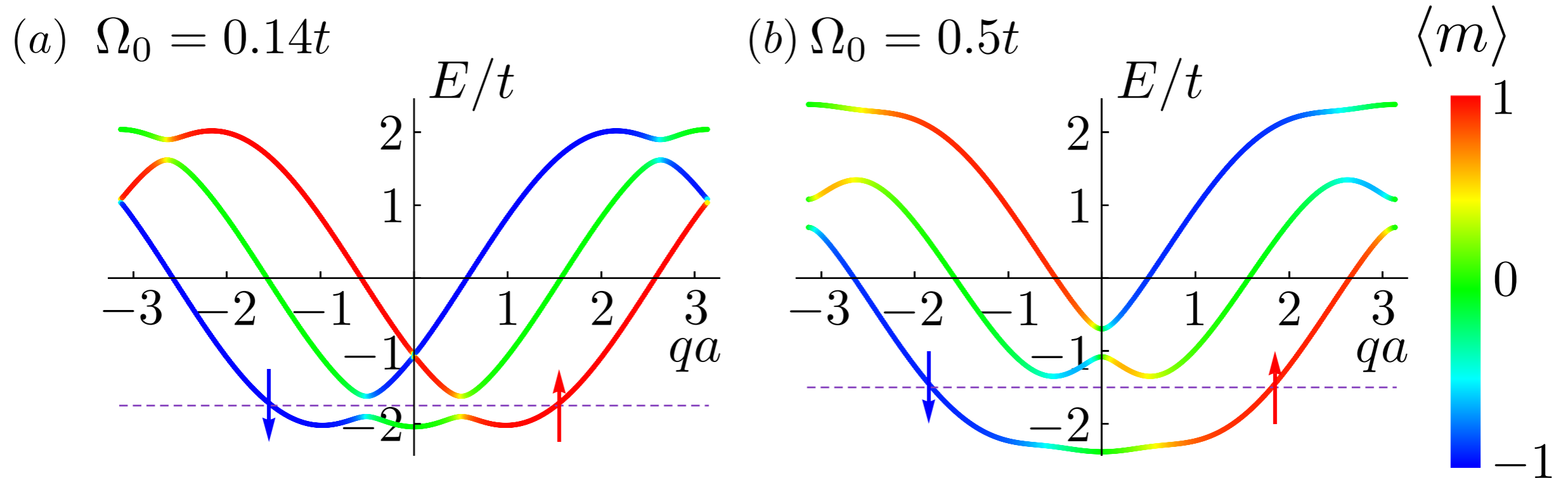
Yields:

- laser-assisted, position-dependent complex spin-tunnellings
- non-staggered magnetic flux  $\Phi$  (and large, easily up to  $\pi$ -flux!)
- “ $\infty$ -ranged” interactions



Celi, PM, Ruseckas, Goldman, Spielman, Juzeliunas, and Lewenstein, PRL (2014)

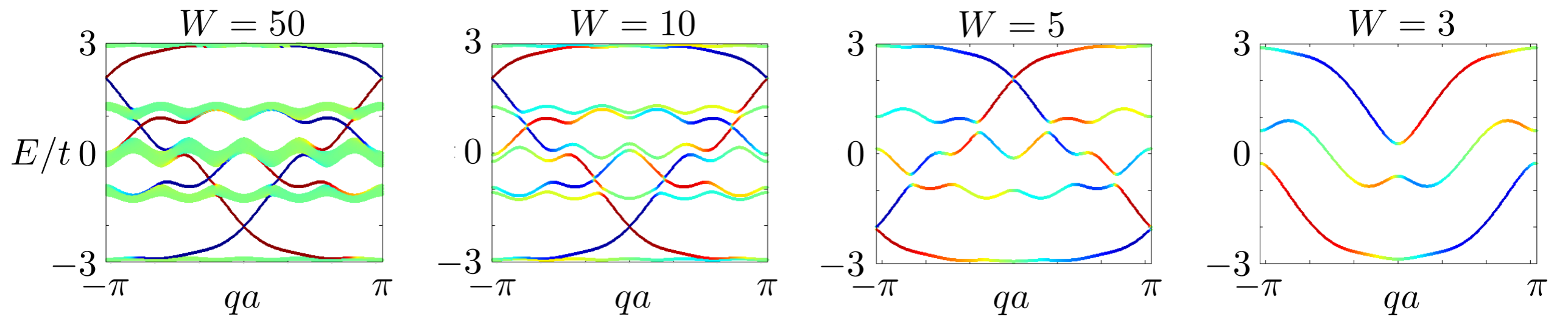
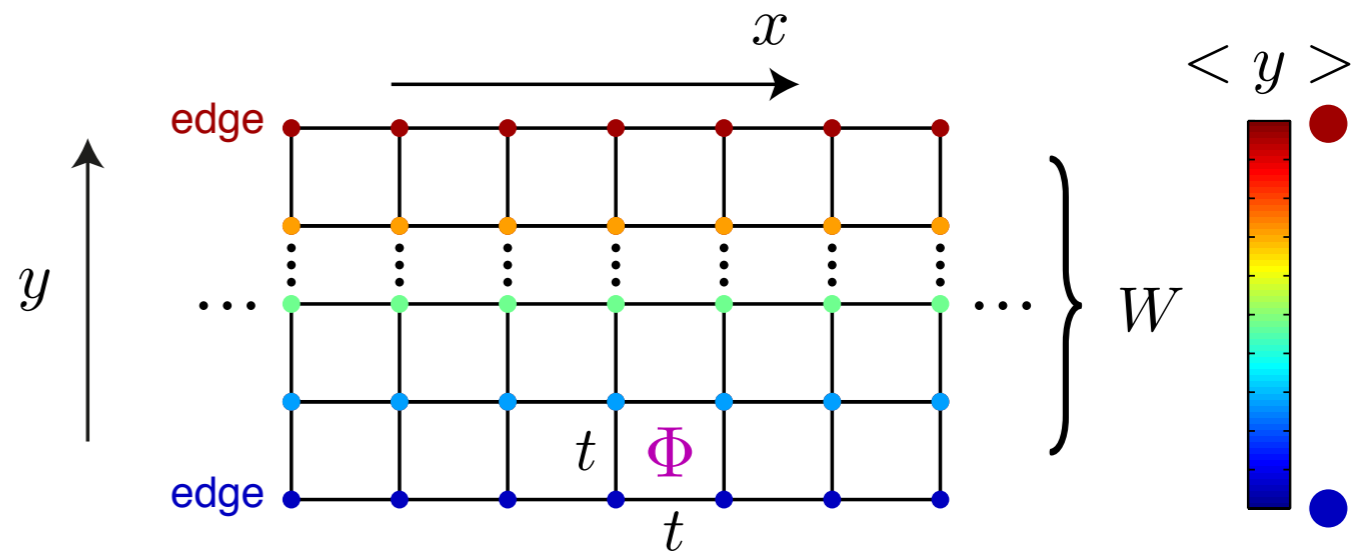
# Spectrum with 3 internal states



States inside the Raman-gap have  $\langle m \rangle \approx \pm 1$   
i.e., are **chiral edge states on the synthetic lattice**  
(analogous to those found in QH systems)

# Hofstadter strip

Our system continuously connects to the textbook problem of a regular 2D square lattice, pierced by a uniform magnetic field:



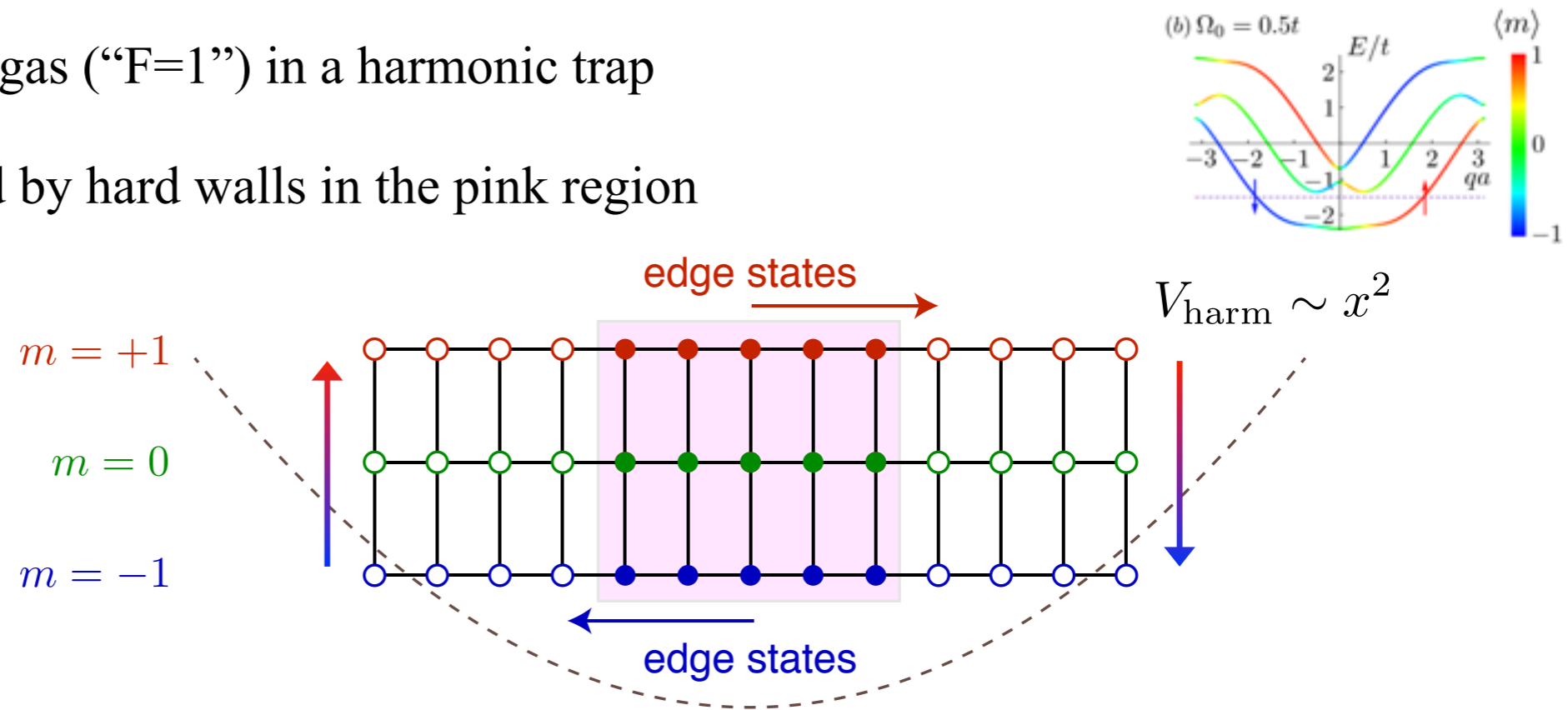
$$\Phi = 1/5$$



# Edge state dynamics

A three-component Fermi gas (“F=1”) in a harmonic trap

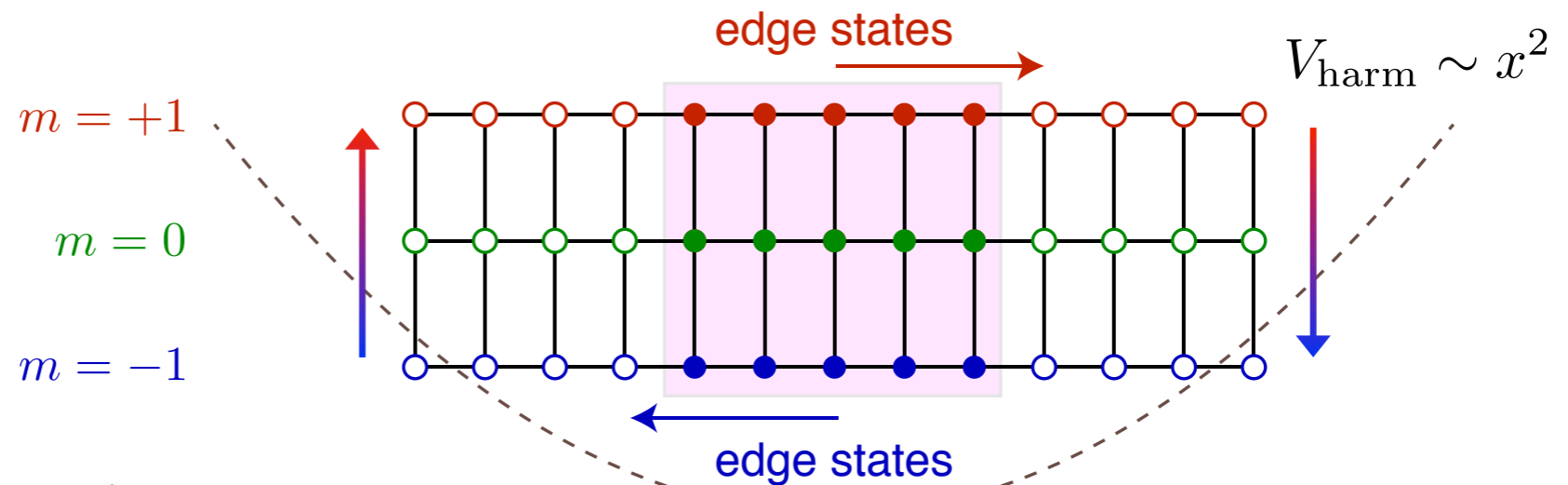
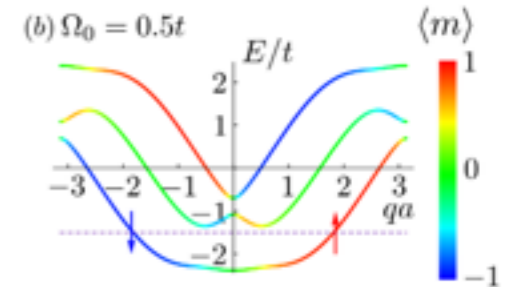
for  $t < 0$ , the gas is confined by hard walls in the pink region



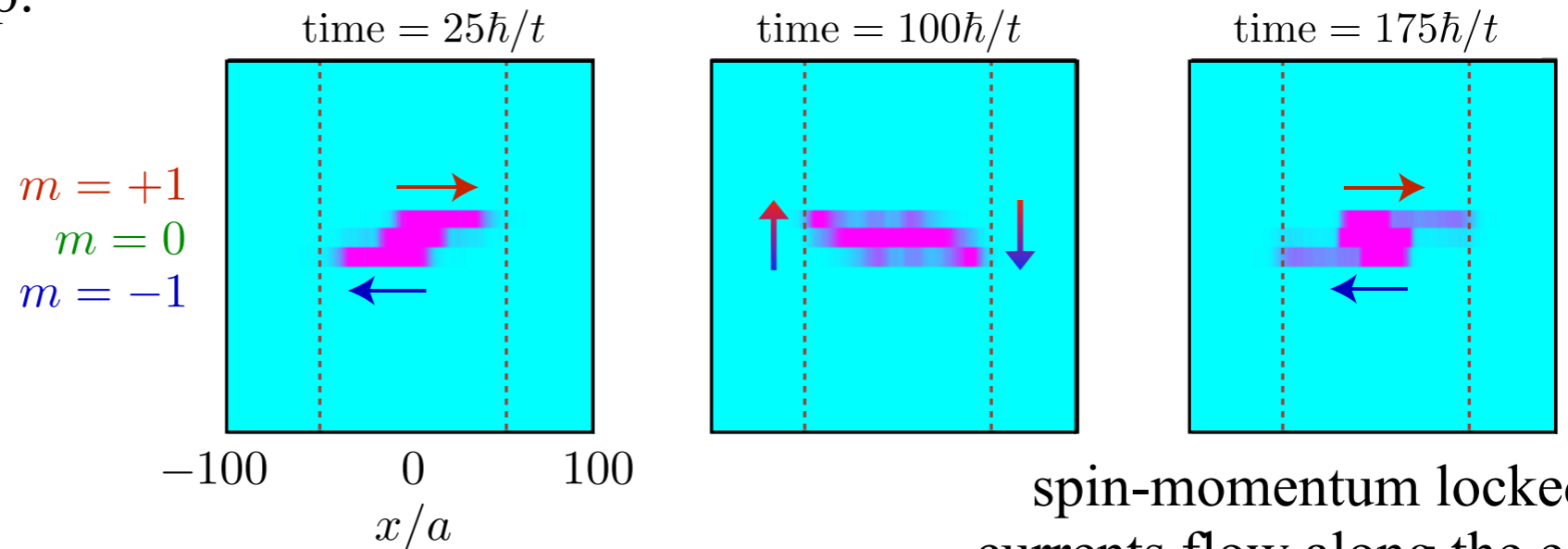
# Edge state dynamics

A three-component Fermi gas (“F=1”) in a harmonic trap

for  $t < 0$ , the gas is confined by hard walls in the pink region



remove the “pink” confinement,  
but leave the harmonic trap:



$$\Omega_0 = 0.5t$$

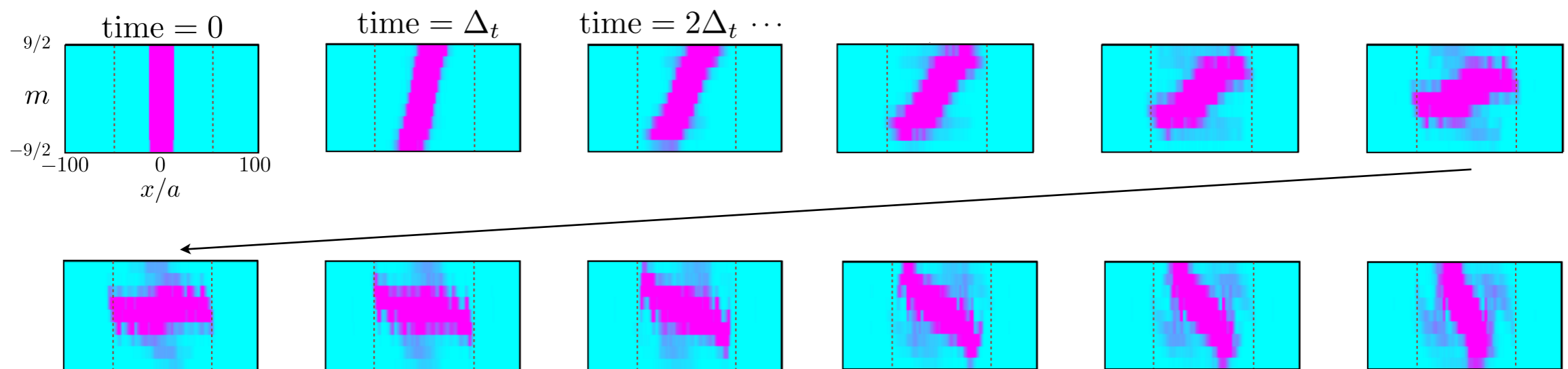
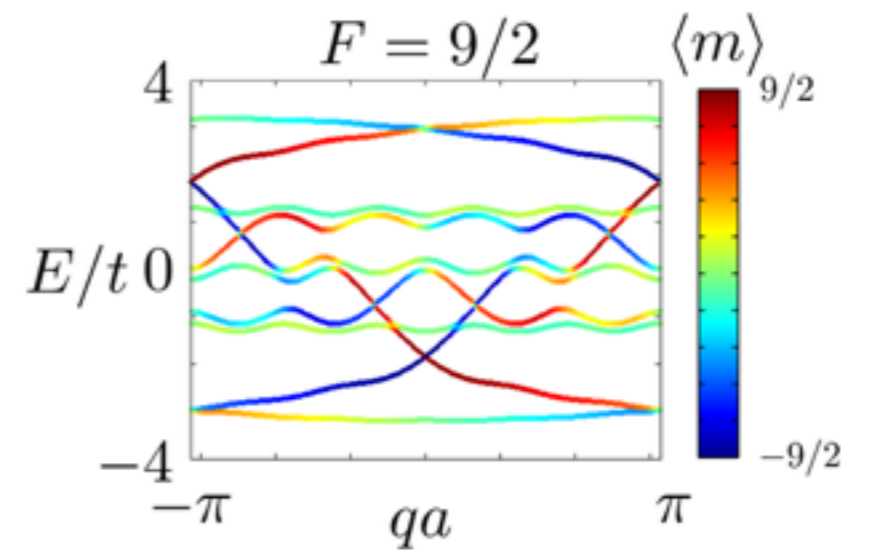
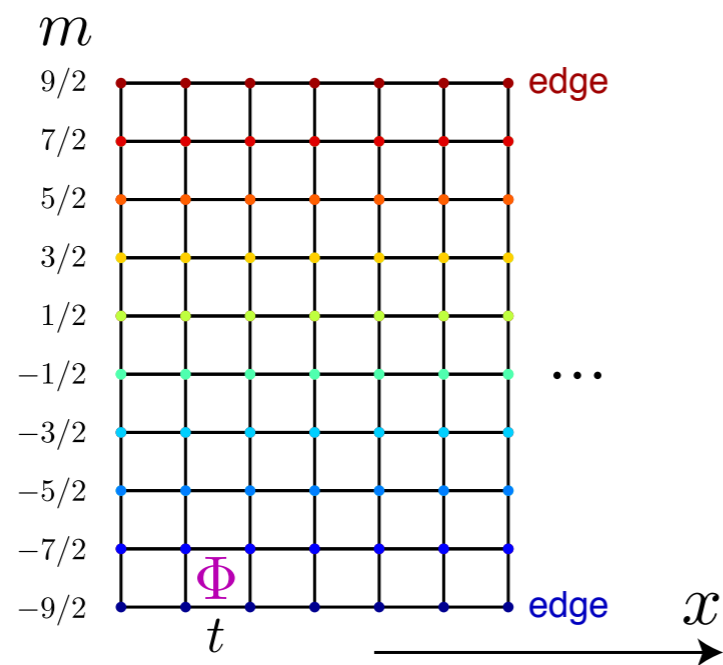
$$\Phi = 1/2\pi$$

$$E_F = -1.4t$$

spin-momentum locked  
currents flow along the edge

# Edge state dynamics for $^{40}\text{K}$

(10 internal states)

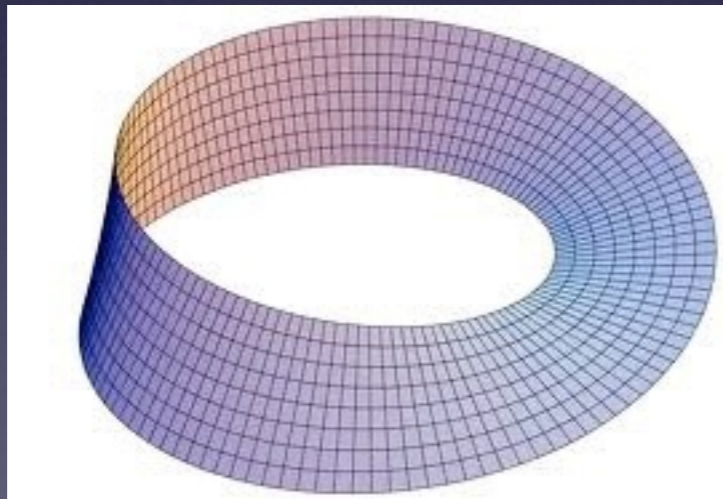
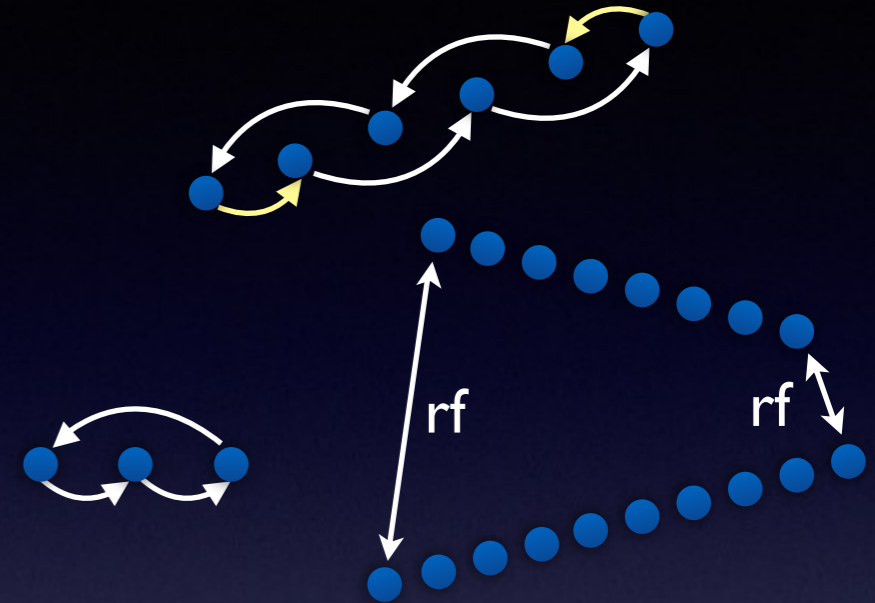


# Interesting topologies

possible boundary conditions  
along the spin direction:

- open
- closed
- twisted

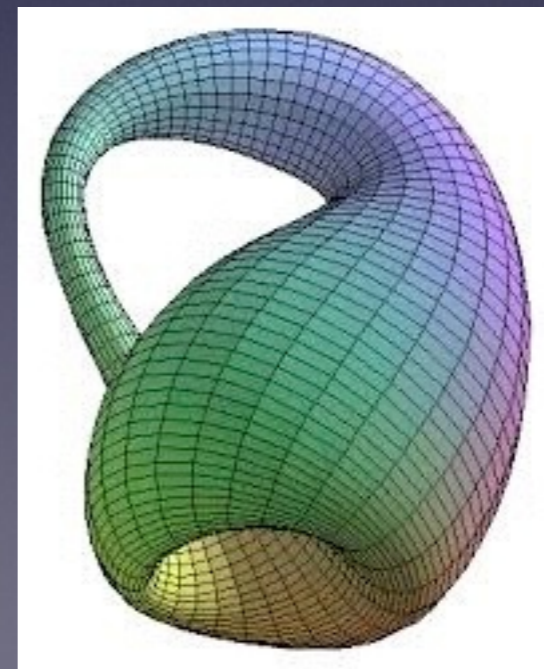
$$m_F = \begin{array}{ccc} \bullet & \bullet & \bullet \\ \curvearrowright & \curvearrowright & \curvearrowright \\ -1 & 0 & 1 \end{array}$$



**Möbius strip**  
linear chain in the spatial dir.,  
 $\pi/2$  twist in spin

## Klein bottle

ring in the spatial dir.,  
 $\pi/2$  twist in spin

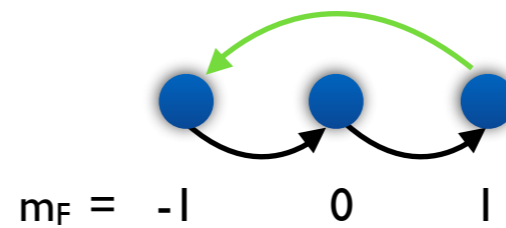


# From open to closed b.c.



+

close the spin-dimension

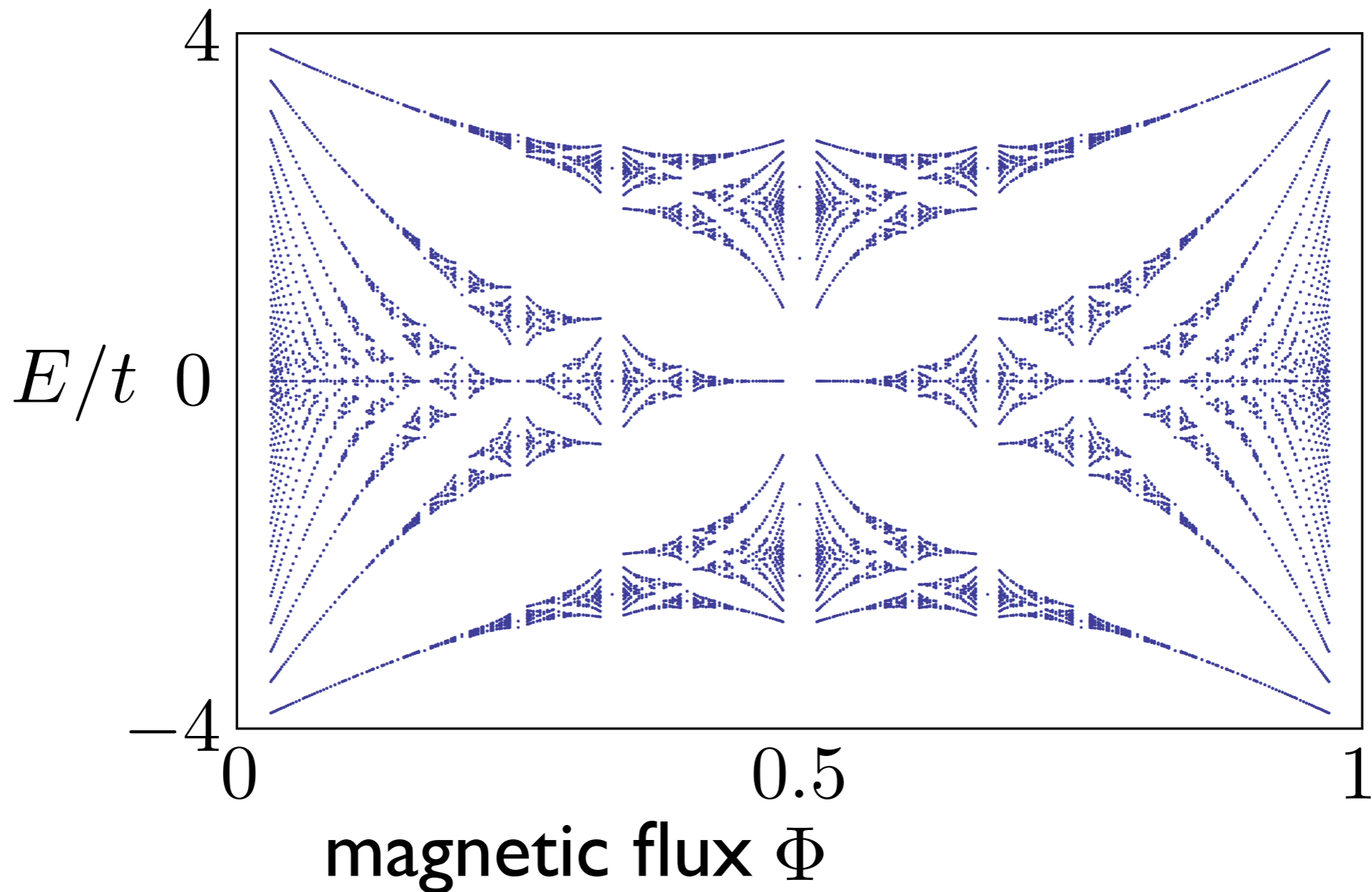


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# Spectrum of a 3-component gas with closed b.c.

The spectrum has the fractal structure of a **Hofstadter butterfly**:



# Outlook / Conclusions

- Q. gases: an ideal arena for topological properties
- Exploiting an internal d.o.f. as an extra-dimension:
  - ★ uniform and large fluxes
  - ★ direct imaging of edge states and their helicity
  - ★ Hofstadter fractal spectrum
- Role of interactions on edge state robustness
- Simulations of Quantum Random Walks
- Quantum simulation of high-energy theories, and 4D systems (e.g., critical exponents of phase transitions)

Celi, PM, Ruseckas, Spielman, Juzeliunas, and Lewenstein

*Synthetic gauge fields in synthetic dimensions*

Phys. Rev. Lett. **112**, 043001 (2014)

